

Student: _____
Date: _____
Time: _____

Instructor: Lance Burger
Course: Math 76 Calculus 2
Book: California State University, Fresno:
Math 75: Calculus

Assignment: Team Test 1 (20 points possible)

1. The table shows the velocity of a remote controlled race car moving along a dirt path for 8 seconds. Estimate the distance traveled by the car using 8 subintervals of length 1 with left-end point values.

Time (sec)	Velocity (in. / sec)
0	0
1	10
2	17
3	13
4	23
5	26
6	28
7	12
8	5

- ☐ A. 258 in
☐ B. 129 in
☐ C. 119 in
☐ D. 134 in

2. Use a finite approximation to estimate the area under the graph of the given function on the stated interval as instructed.

$f(x) = \frac{1}{x}$ between $x = 1$ and $x = 7$, using the midpoint sum with two rectangles of equal width

- ☐ A. $\frac{584}{3025}$
☐ B. $\frac{96}{55}$
☐ C. $\frac{876}{3025}$
☐ D. $\frac{32}{55}$

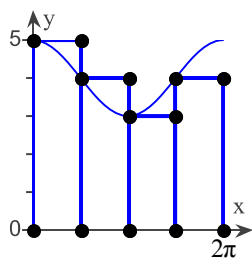
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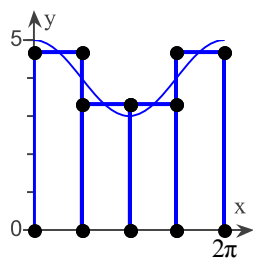
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3. Graph the function $f(x) = \cos x + 4$ over the interval $[0, 2\pi]$. Partition the interval into 4 subintervals of equal length. Then add to your sketch the rectangles associated with the Riemann sum $\sum_{k=1}^4 f(c_k) \Delta x_k$, using the midpoint in the k th subinterval for c_k .

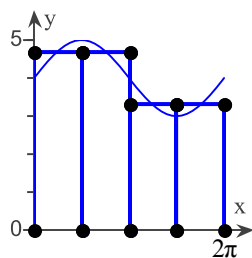
☐ A.



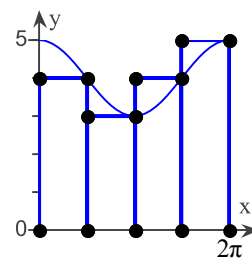
☐ B.



☐ C.



☐ D.



4. Graph the integrand and use geometry to evaluate the integral.

$$\int_{-3}^3 (|x| + 6) dx$$

☐ A. 54

☐ B. 81

☐ C. 45

☐ D. 15

5. Suppose that f and g are continuous and that $\int_6^{10} f(x) dx = -5$ and $\int_6^{10} g(x) dx = 10$.

Find $\int_{10}^6 [g(x) - f(x)] dx$.

☐ A. 5

☐ B. 15

☐ C. -15

☐ D. -5

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6. Suppose that g is continuous and that $\int_1^5 g(x) dx = 8$ and $\int_1^{10} g(x) dx = 13$. Find $\int_{10}^5 g(x) dx$.

- ☐ A. -21
☐ B. 5
☐ C. -5
☐ D. 21

7. Evaluate the integral.

$$\int_0^{\pi} \frac{3 - \sin 8x}{8} dx$$

- ☐ A. $\frac{3\pi}{8} - \frac{1}{16}$
☐ B. $\frac{3\pi}{8}$
☐ C. $\frac{3\pi}{8} + \frac{1}{16}$
☐ D. $-\frac{3\pi}{8}$

8. Find the derivative.

$$\frac{d}{dx} \int_1^{\sqrt{x}} 18t^7 dt$$

- ☐ A. $12x^3$
☐ B. $9x^3$
☐ C. $\frac{9}{2}x^3 - \frac{9}{2}$
☐ D. $18x^{7/2}$

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9. Find the average value of the function over the given interval.

$$f(x) = 10x \text{ on } [7,9]$$

- ☐ A. 320
☐ B. 40
☐ C. 80
☐ D. 160

10. Find the average value of the function over the given interval.

$$y = x^2 - 3x + 6; [0,6]$$

- ☐ A. 6
☐ B. 39
☐ C. 9
☐ D. 24

11. Find the values(s) of x at which the given function equals its average value on the given interval.

$$f(x) = |x|; [0,4]$$

- ☐ A. $\frac{5}{2}$
☐ B. 2
☐ C. 3
☐ D. 1

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12. Use the substitution formula to evaluate the integral.

$$\int_0^{7\pi/4} \tan \frac{x}{7} dx$$

- ☐ A. $\frac{-7\sqrt{2}}{2}$
☐ B. $\frac{7 \ln 2}{2}$
☐ C. $\frac{-7 \ln 2}{2}$
☐ D. $\frac{7\sqrt{2}}{2}$

13. Find the area of the region between the curve $y = 6x/(1 + x^2)$ and the interval $-2 \leq x \leq 2$ of the x-axis.

- ☐ A. $6 \ln 5$
☐ B. $\ln 5$
☐ C. $6e^5$
☐ D. 0

14. Find the area of the region between the curve $y = 5^{3-x}$ and the interval $0 \leq x \leq 2$ on the x-axis.

- ☐ A. $120 \ln 5$
☐ B. $\frac{120}{\ln 5}$
☐ C. $\frac{125}{\ln 5}$
☐ D. 125

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15. Evaluate the integral by using multiple substitutions.

$$\int 7(3x^2 - 6) \sin^5(x^3 - 6x) \cos(x^3 - 6x) dx$$

- ☐ A. $\frac{6}{7} \sin^6(x^3 - 6x) + C$
☐ B. $\frac{7}{6} \cos^6(3x^2) + C$
☐ C. $35 \sin^4(x^3 - 6x) + C$
☐ D. $\frac{7}{6} \sin^6(x^3 - 6x) + C$

16. (This problem is worth 5 pts!) Show all work for full credit.
Using the definition of the definite integral as an infinite limit of the Riemann sum, prove that:

$$\int_0^1 x^2 - 2x + 1 \, dx = \frac{1}{3}.$$

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1. B

2. B

3. B

4. C

5. C

6. C

7. B

8. B

9. C

10. C

11. B

12. B

13. A

14. B

15. D

16.